

## Using constraint solvers to support metamorphic testing

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# Context

## Context

- Metamorphic Testing(MT)
- Metamorphic Relations(MRs)
- Systematic MRs identification and validation

## Target

- Represent MRs as a set of constraint
  - Constraint solvers
  - Select MiniZinc
  - Apply to a case study

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# Fundamentals

## Constraint Programs Systems (CPS)

- 90s: Constraint Logic Programming (CLP)
- Constraint Programs Systems CPS
- MiniZinc

## Constraint solving and MT

- Prototype implementation using INKA test case generator (2003, Gotlieb and Botella)
- MT to validate the Minion CPS (2018, Akgün et al. )

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# The MiniZinc language

## Features

- Open source constraint language
- Uses: model constraint satisfaction and optimization
- Separate data and model files





## The MiniZinc language (II)

---

```
% Colouring Andalusia using this many colours      1
int: nc = 3;                                       2
                                                    3
var 1..nc: al; var 1..nc: ca; var 1..nc: co;      4
var 1..nc: gr; var 1..nc: hu; var 1..nc: ja;      5
var 1..nc: ma; var 1..nc: se;                     6
                                                    7
constraint al != gr; constraint gr != ja;         8
constraint gr != co; constraint gr != ma;         9
constraint ja != co; constraint co != ma;        10
constraint co != se; constraint ma != ca;        11
constraint ma != se; constraint se != ca;        12
constraint se != hu;                               13
                                                    14
solve satisfy ;                                    15
                                                    16
output ["al =\ (al )\ t_ca=\ (ca )\n",            17
          "co=\ (co )\ t_gr=\ (gr )\ t_<hu=\ (hu)\n", 18
          "ja =\ (ja )\ t_ma=\ (ma)\n",            19
          "se_=", show(se), "\n"];                20
```

---

Listing 1. Sample MiniZinc model

## The MiniZinc language (III)

- Parameter definition
- Variable declarations
- Constraints
- *solve* (satisfaction or minimization/maximization)

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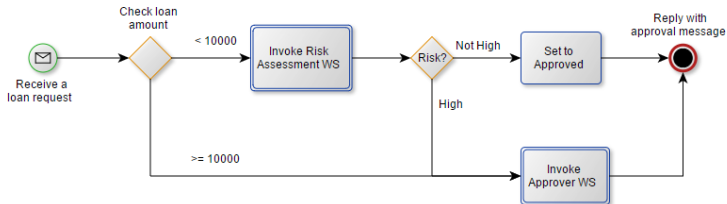
## Mapping MR to MiniZinc

- Decision variable and parameter declarations (initial and follow-up test cases)
- A set of constraints over previous decision variables and parameters

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# Loan Approval Example



- Low amount ( $< 10,000$ )
  - Low Risk
  - High Risk
- High amount ( $\geq 10,000$ )

# Notation

We recall that each MR relates an initial test case (here it is represented by 1) to a subsequent test case (here it is represented by 2). The elements of each test case are:

- `req_amountN` is the amount requested by the customer,  $N$  can be 1 or 2 (depending on the initial case or the next case, generated by the MR)
- `ap_replyN` is the response from the approver service (“true” if approved, “false” if not)
- `as_replyN` is the assessor’s response (“true” is high, “false” is low)
- `accepted` is the final answer given to the customer

## Some MRs

- **MR1.2** (increasing low amount):

$$req\_amount2 = req\_amount1 * 10 \wedge req\_amount1 < 10000 \wedge req\_amount2 < 10000 \wedge ap\_reply2 = ap\_reply1 \wedge as\_reply2 = as\_reply1 \implies accepted2 = accepted1$$

- **MR2.1** (reducing high amount):

$$req\_amount2 = req\_amount1 / 2 \wedge req\_amount1 \geq 10000 \wedge req\_amount2 \geq 10000 \wedge ap\_reply2 = ap\_reply1 \wedge as\_reply2 = as\_reply1 \implies accepted2 = accepted1$$

- **MR3** (negating the approver on a high amount):

$$req\_amount2 = req\_amount1 \wedge req\_amount1 \geq 10000 \wedge ap\_reply2 = not(ap\_reply1) \wedge as\_reply2 = as\_reply1 \implies accepted2 = not(accepted1)$$

- **MR4** (negating the assessor on a high amount):

$$req\_amount2 = req\_amount1 \wedge req\_amount1 \geq 10000 \wedge ap\_reply2 = ap\_reply1 \wedge as\_reply2 = not(as\_reply1) \implies accepted2 = accepted1$$



## New test cases generation

Once the satisfiability of the proposed MRs has been checked, this section tries to use these MRs to generate new test cases (the follow-up test cases). This is the traditional use of MRs in the MT technique

- For high amounts, (`amount = 15000`, `ap_reply = true`, `as_reply = false`, `accepted = true`) was used. While the common model file requires a value for `as_reply`, this value did not impact executions: the assessor is not used for large amounts
- For low amounts, there are two options: low risk or high risk. For low risk, (`amount = 150`, `ap_reply = false`, `as_reply = false`, `accepted = true`) could be used with MR1.2 and MR2.2. For high risk, (`amount = 15000`, `ap_reply = false`, `as_reply = true`, `accepted = false`) was used with MR1.3

## Generating new cases

---

```
1  % PARAMETERS (OLD TEST CASE)
2  int: req_amount1;
3  bool: ap_reply1;
4  bool: as_reply1;
5  bool: accepted1;
6
7  % VARIABLES (NEW TEST CASE)
8  var int: req_amount2;
9  var bool: ap_reply2;
10 var bool: as_reply2;
11 var bool: accepted2;
12
13 %% COMPOSITION-SPECIFIC CONSTRAINTS
14 constraint req_amount1 >= 0;
15 constraint req_amount2 >= 0;
```

---

Listing 1: Common MiniZinc model for LoanApproval

## Generating new cases

---

```
include "loanAp_common.mzn";

%% MR-SPECIFIC CONSTRAINTS
constraint req amount1 < 10000 ;
constraint req amount2 < 10000 ;
constraint req_amount2 = req_amount1 * 10;
constraint ap_reply2 = ap_reply1;
constraint as_reply2 = as_reply1;
constraint accepted2 = accepted1;
```

---

Listing 2: MiniZinc model of MR1.2 (increasing low amount) of LoanApproval

## Generating new cases

---

```
include "loanAp_common.mzn";

%% MR-SPECIFIC CONSTRAINTS
constraint req_amount1 >= 10000 ;
constraint req_amount2 = req_amount1;
constraint ap_reply2 = ap_reply1;
constraint as_reply2 = not as_reply1;
constraint accepted2 = accepted1;
```

---

Listing 3: MiniZinc model of MR4 (negating the assessor on a high amount) of LoanApproval

## Generating new cases

---

```
% VARIABLES (OLD TEST CASE)
var int: req_amount1;
var bool: ap_reply1;
var bool: as_reply1;
var bool: accepted1;

% VARIABLES (NEW TEST CASE)
var int: req_amount2;
var bool: ap_reply2;
var bool: as_reply2;
var bool: accepted2;

%% COMPOSITION-SPECIFIC CONSTRAINTS
constraint req_amount1 >= 0;
constraint req_amount2 >= 0;
```

---

Listing 4: Common MiniZinc model of LoanApproval with variables

## Test cases generation tables

TABLE II  
GENERATED TESTS, WITH SOURCE MRS (HIGH AMOUNT)

MR	Initial test case	Following test case
MR1 . 1	(15000, true, true, true)	(150000, true,true, true)
MR2 . 1	(15000, true, true, true)	(7500, true,true, true)
MR3	(15000, true, true, true)	(15000, false,true, false)
MR4	(15000, true, true, true)	(15000, true, false, true)

TABLE III  
GENERATED TESTS, WITH SOURCE MRS (LOW AMOUNT)

MR	Initial test case	Following test case
MR1 . 2	(150, false, false, true)	(1500, false,false, true)
MR2 . 2	(150, false, false, true)	(75, false, false, true)
MR1 . 3	(1500, false, true, false)	(15000, false, false, false)

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# MuBpel

## Steps

- 1 The composition was analyzed
- 2 All possible mutants were generated
- 3 The original composition, initial test case, collecting its outputs
- 4 The mutants were executed
- 5 The original composition, following test cases, collecting its outputs
- 6 The remaining mutants were executed. The following test cases, and their outputs were compared against those of the original composition



# Results

TABLE IV  
MUBPEL VALIDATION RESULTS

Suite	Total	Killed	Alive	# tests
Initial	96	50	46	3
Follow-up	96	84	12	3 + 7

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# Conclusions

## Conclusions

- Challenges in MT
- Proposal of representing MRs through MiniZinc
- A case of study has been presented
- It has been checked through mutation testing
- The following tests cases were be able to detect 34 defect

## Future work

- Further improve defect detection
- Larger and more complex programs

# Thanks

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